

# **Ocean Wave Data Analysis**

Introduction to Time Series Analysis,  
Signal Processing, and Wave Prediction

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